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### **Application to Metal Oxidation**

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## Introduction



**Nuclear Power Plant** 

**Picture AREVA NP** 

**FUEL** 

Fuel assembly

Picture AREVA NP

### Understanding corrosion key factor impact on oxide growth

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## **Objectives**

- Develop a numerical model for zirconium oxidation
- Simulation using <u>COMSOL Multiphysics</u>

### Multicomponent transport coupled with internal chemical reaction



**Constraints on system :** 

**Electroneutrality + Stoichiometry + Chemical reaction** 

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# **Conservative Ensembles**

### Considering ensemble transport (J. Maier, 1994)



Thermodynamic of irreversible processes

$$J_{O}^{*} = -s_{OO}^{*} \nabla \eta_{O}^{*} - s_{Oe}^{*} \nabla \eta_{e}^{*}$$
$$J_{e}^{*} = -s_{eO}^{*} \nabla \eta_{O}^{*} - s_{ee}^{*} \nabla \eta_{e}^{*}$$

(Lankhorst, 1996)

Ensembles are conservatives for the chemical reaction

### Chemical reaction : Cross effect between ensembles fluxes

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# **Oxygen Flux**

Oxygen flux given by: (Wagner, 1977)

$$J_o = \frac{-\sigma_{amb}}{4F^2} \nabla \mu_o = -D^{\delta} \nabla c_o$$

**Chemical diffusion coefficient** 

$$D^{\delta} = \frac{\sigma_{amb}}{4F^2} \left(\frac{d\mu_0}{dc_0}\right)$$

 $\sigma_{amb}$  : Ambipolar conductivity  $rac{d\mu_{o}}{dc_{o}}$  : Chemical capacity

**Constraints on system** 

$$\begin{aligned} c_{V_{O}^{\bullet}} + 2c_{V_{O}^{\bullet\bullet}} - c_{e'} &= 0 & \text{Electroneutrality} \\ \partial c_{O} + \partial c_{V_{O}^{\bullet\bullet}} + \partial c_{V_{O}^{\bullet}} &= 0 & \text{Stoichiometry} \\ K &= \frac{c_{V_{O}^{\bullet\bullet}} c_{e'}}{c_{V_{O}^{\bullet}}} & \text{Chemical Reaction} \end{aligned}$$

Transport equation:

$$\frac{\partial c_o}{\partial t} = \nabla D^{\delta} \nabla c_o$$

All system's information are given by  $D^{\delta}$ 



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# **Oxide Growth**

Oxide growth given by:



Boundary condition on internal interface

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Keeping subdomain constant: 
$$x_{reduced} = \frac{x_{real}}{e_{ox}}$$
;  $\nabla |_{real} = \frac{1}{e_{ox}} \nabla |_{reduced}$ 

Oxide growth model formulated as <u>boundary weak form</u>

#### Simulation in one dimension:



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## **Oxide Growth**

### **Model parameters**

Symbol	Description
K	Chemical equilibrium between vacancies
D <sub>V</sub> ••	Diffusion coefficient of vacancies V**
$D_{V^{\bullet}}$	Diffusion coefficient of vacancies V•
D <sub>e</sub>	Diffusion coefficient of electrons
$\delta_{int}$	Zirconia non stoichiometry at the M/O interface
δ <sub>ext</sub>	Zirconia non stoichiometry at the surface
Т	Temperature



## Simulations

### **Comparison with experimental data**







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## Simulations

### Effect on reaction and transport coefficient





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## Simulations

### Effect on zirconia non stoichiometry on inner interface ZrO<sub>2-δ</sub>







# Conclusions

• Development of an oxide growth model for anionic transport

Model is not specific for zirconium oxidation

• Assessment of the control parameters on growth kinetics

Transport coefficient, stoichiometry, ...

### Environmental effect could be add on the model

2D model version when symmetry is broken





## Thank you for your attention !

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