



Presented at the 2011 COMSOL Conference

# Opto-Mechanical Surface Acoustic Waves on Micro-sphere

Captain John D. Zehnpfennig II

Photonics Research Center

United States Military Academy, West Point, NY

This work was performed under the guidance of Prof. Tal Carmon and Dr. Gaurav Bahl while Captain Zehnpfennig completed his M.S.Eng. Thesis at the University of Michigan, Ann Arbor



# Motivation

- Surface Opto-mechanics pushing toward quantum limits of measurement
- Cheap, non-toxic local oscillation
- Cheap, easy to deploy chemical detectors to benefit machine olfactorization



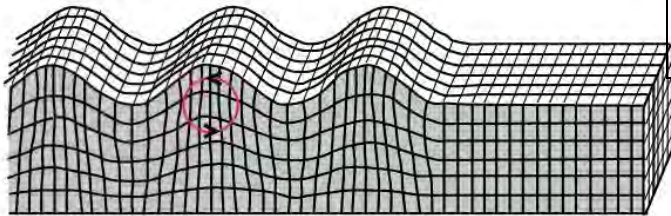
# Agenda

- Opto-mechanical Theory
- Opto-mechanical Interaction
- Modal Velocities
- High-Order Surface Acoustic Wave Modes
- Experimental Method
- Measured and Simulated Results
- Summary

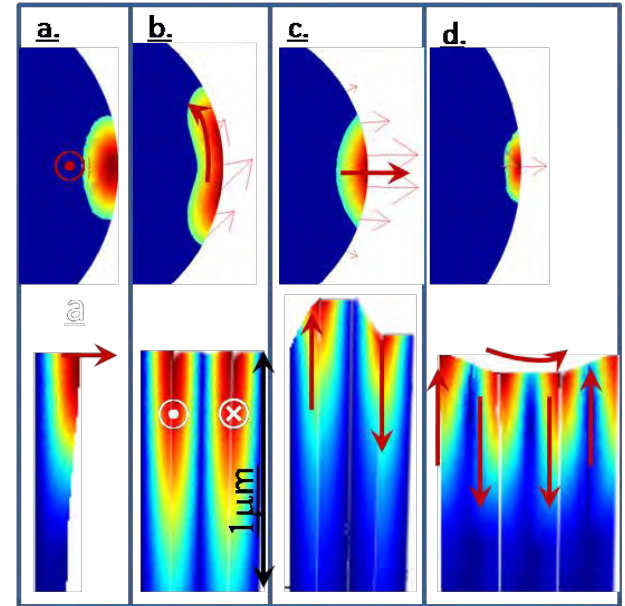
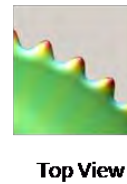
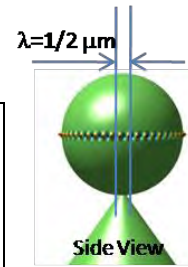
# Theory



Rayleigh Wave

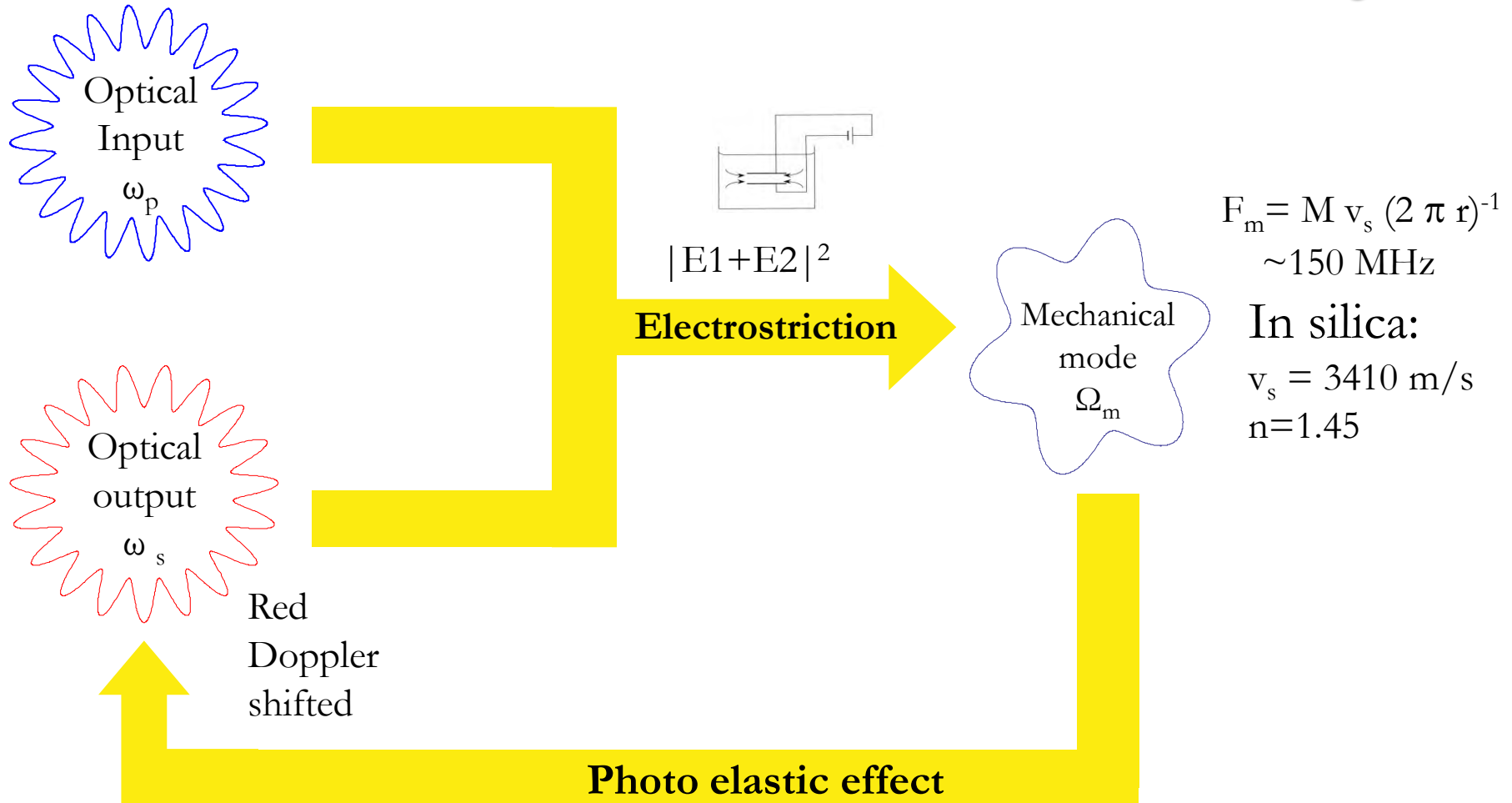


$$k_{\text{mech}} = \frac{1}{2} k_{\text{pump}}$$



Analytic Solution on Bulk SiO <sub>2</sub>		COMSOL Calculation, SiO <sub>2</sub> Sphere, M <sub>φ</sub> =2000		
Wave	Velocity [m/s]	Mode	Deformation	Velocity [m/s]
Longitudinal	$V_L = \left( \frac{E(\nu-1)}{\rho(2\nu^2+\nu-1)} \right)^{1/2} = 5972$	Longitudinal	Azimuthal	5957
Transverse	$V_T = \left( \frac{E}{2\rho(\nu+1)} \right)^{1/2} = 3766$	Transverse	Polar	3787
Rayleigh	$V_R = \frac{V_T(0.87 + 1.12\nu)}{(1 + \nu)} = 3413$	Rayleigh	Radial-Polar	3420

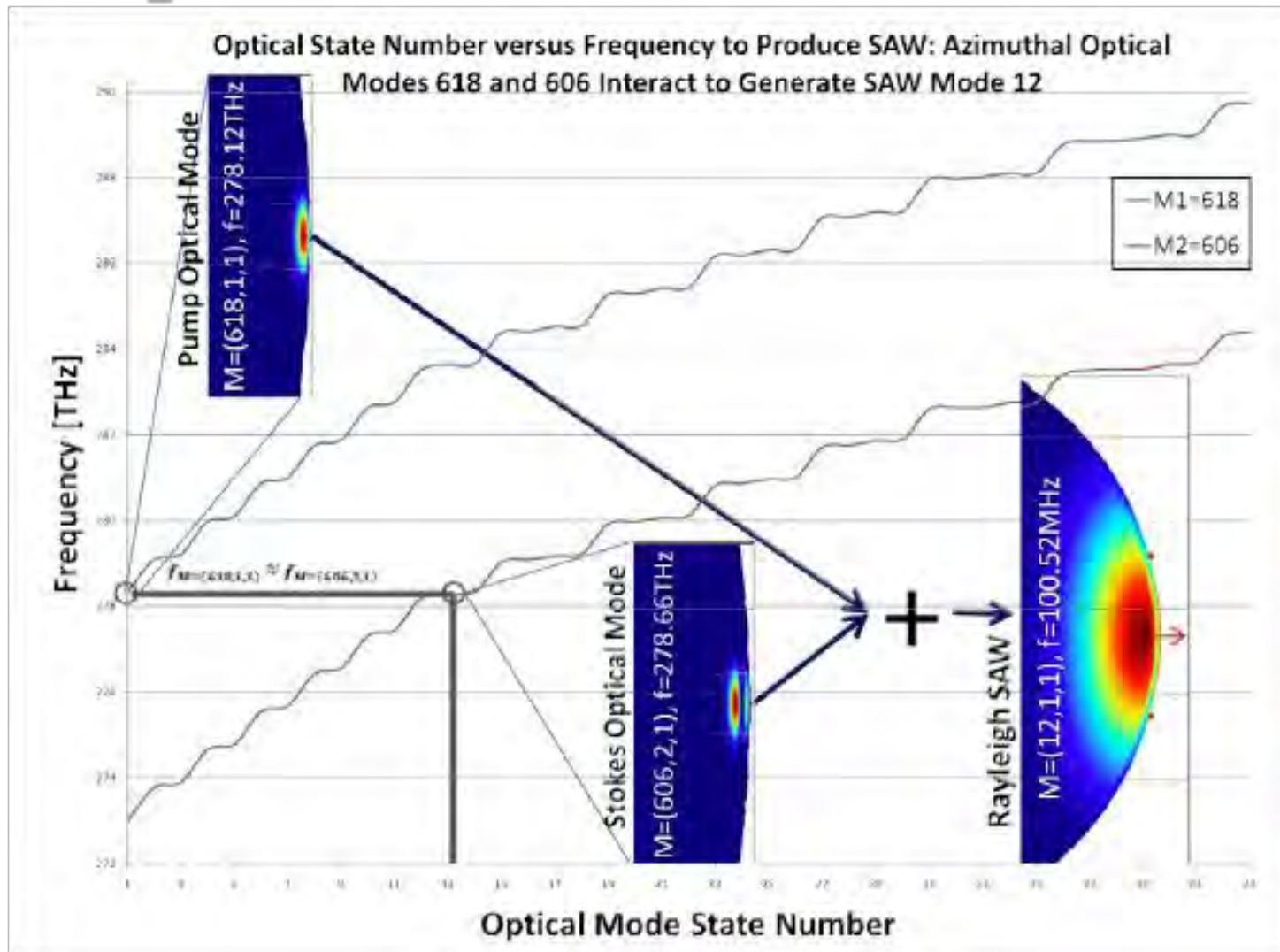
# SAW Mode, Self Consistency



Effective propagation is 100 meters in a micron scaled device

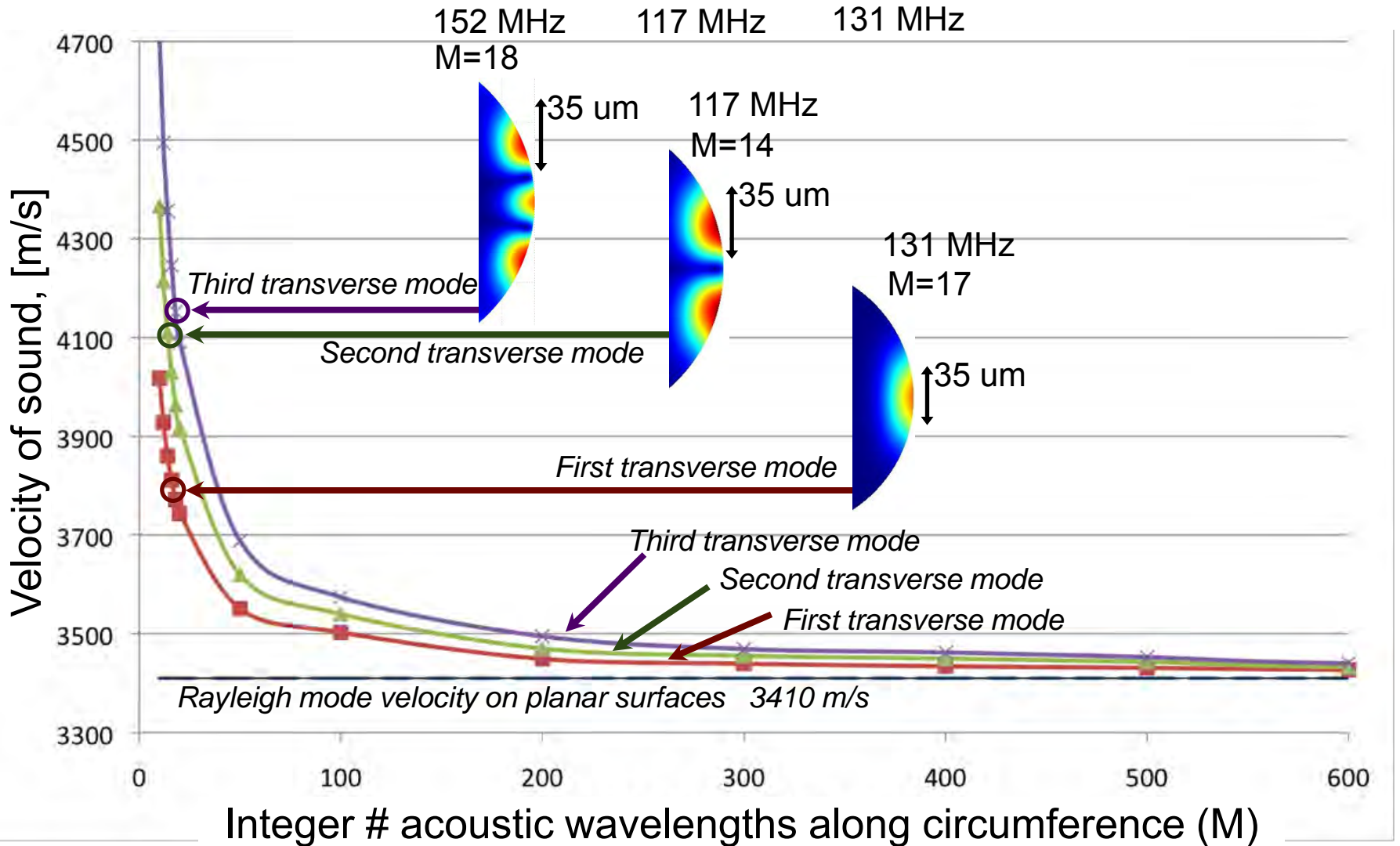
A. Yariv, Quantum Electronics (Wiley, New York, 1975).

# Opto-Mechanical Interaction



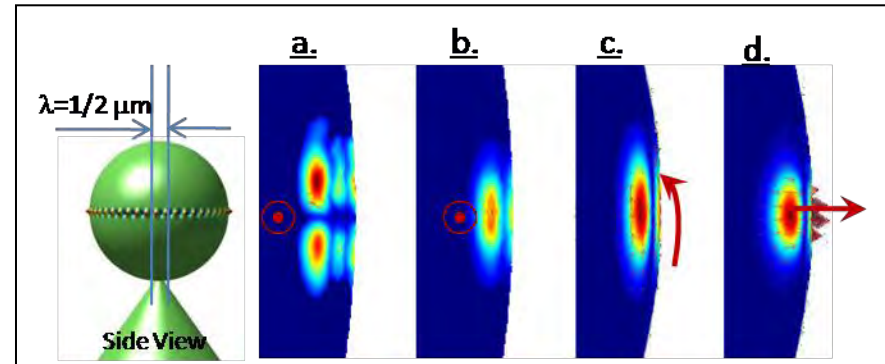
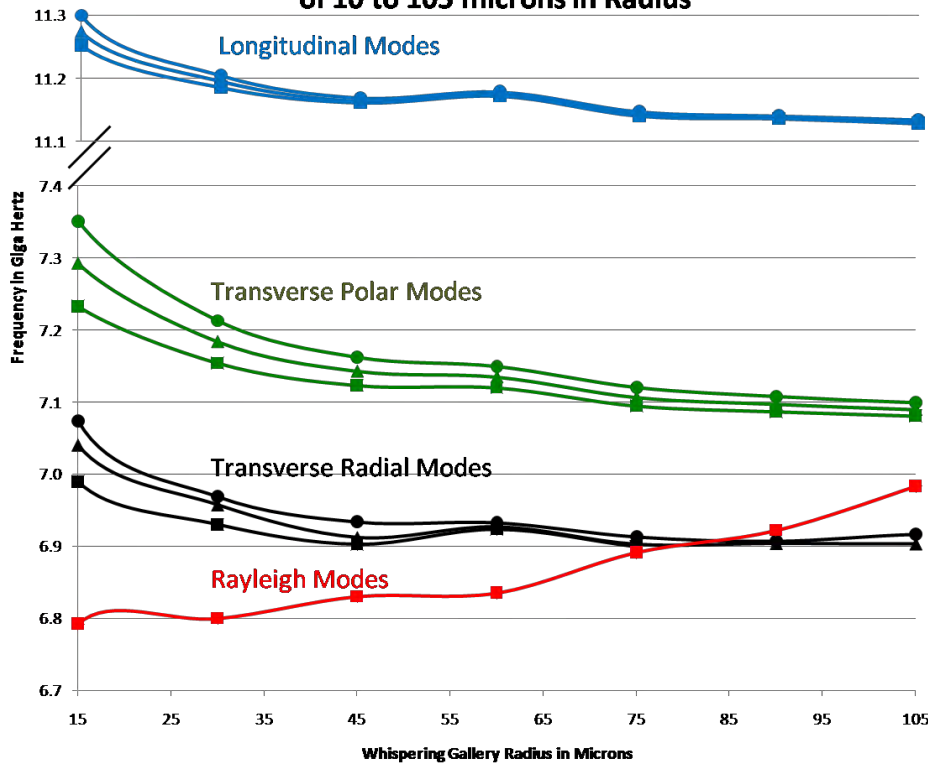


# Modal Velocities



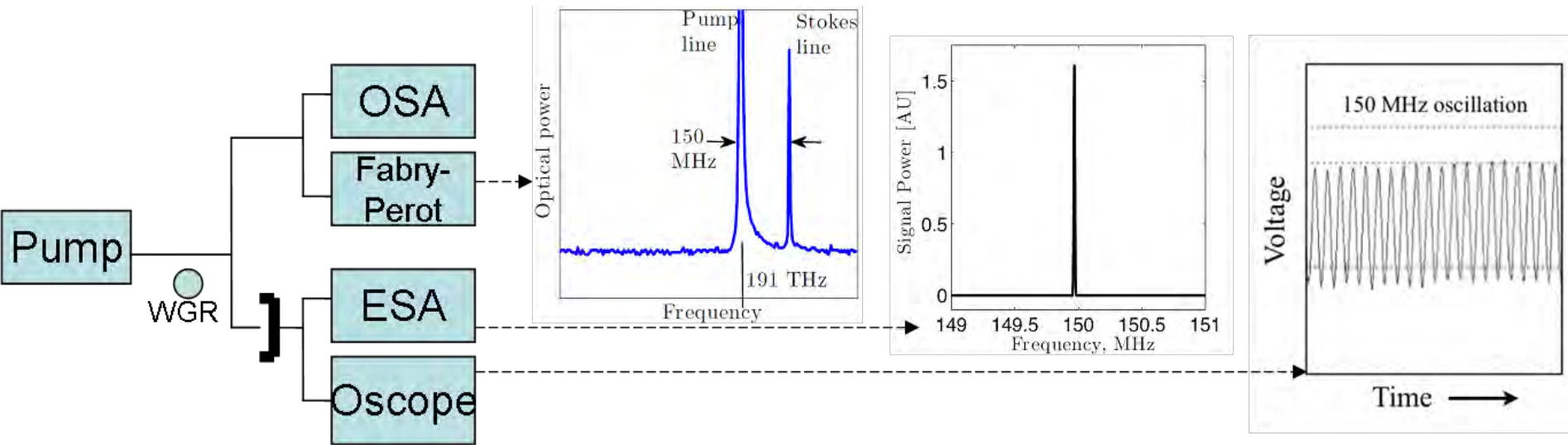
# Modal Spectroscopy – High Order SAW

Surface Acoustic Waves on Spherical WG Resonators  
of 10 to 105 microns in Radius





# Experimental Method



OSA: Optical Spectrum Analyzer

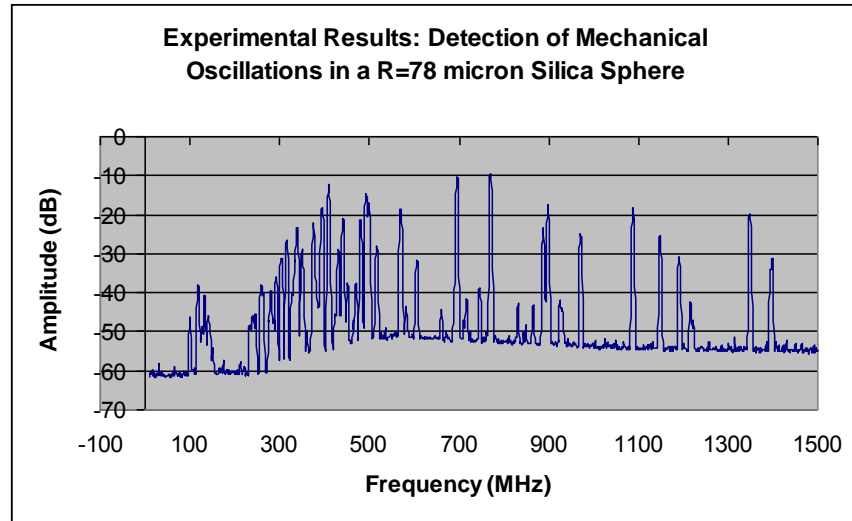
ESA: Electrical Spectrum Analyzer

Pump: wavelength=1.55 micron, continuous wave

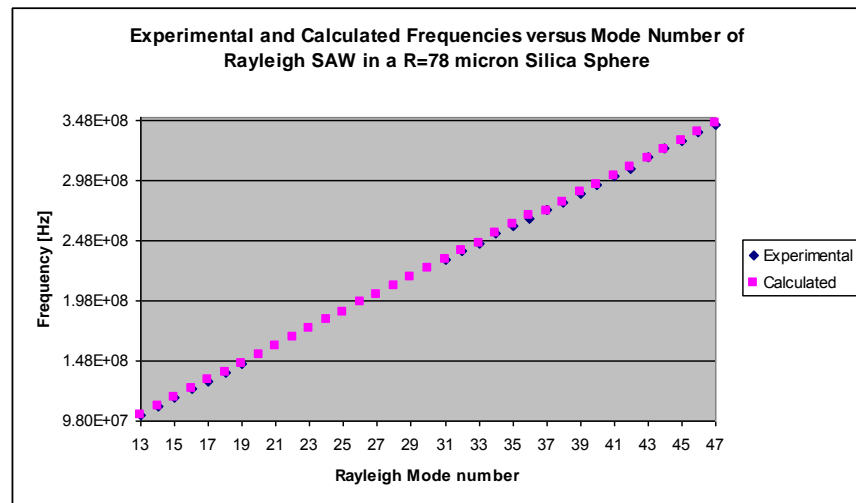
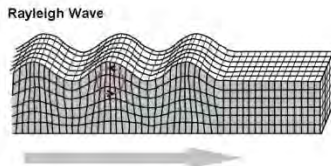
WGR: Whispering Gallery (Micro-)Resonator

# Measured and Simulated Results

Top: Excited SAW Frequencies in a Single WGR



Bottom: Experimental AND Calculated Results: Frequency vs Azimuthal Mode Number





# Summary

- COMSOL Calculated, Analytical, and Experimental results agree within 1%
- COMSOL enabled me to run hundreds of iterations of a simulation automatically – freeing time for the lab



# For Further Info

- [1] L. Rayleigh, *Philos. Mag* 20 (1910) 1001.
- [2] L. Rayleigh, *Proceedings of the London Mathematical Society* 1 (1885) 4.
- [3] T. Carmon, H. Rokhsari, L. Yang, T. J. Kippenberg, and K. J. Vahala, *Physical Review Letters* 94 (2005) 223902.
- [4] Q. Lin, X. Jiang, M. Eichenfield, R. Camacho, P. Herring, K. Vahala, and O. Painter, in *Conference on Lasers and Electro-Optics/International Quantum Electronics Conference 2009*, OSA, Baltimore, Maryland, 2009, p. CMKK1.
- [5] X. Jiang, Q. Lin, J. Rosenberg, K. Vahala, and O. Painter, *Optics Express* 17 (2009) 20911.
- [6] M. Tomes and T. Carmon, *Physical Review Letters* 102 (2009) 113601.
- [7] A. B. Matsko, A. A. Savchenkov, V. S. Ilchenko, D. Seidel, and L. Maleki, *Physical Review Letters* 103 (2009) 257403.
- [8] **J. Zehnpfennig**, M. Tomes, and T. Carmon, in *2010 International Conference on Optical MEMS and Nanophotonics (OPT MEMS)*, IEEE, Sapporo, Japan, 2010, p. 51.
- [9] T. Carmon, H. G. L. Schwefel, L. Yang, M. Oxborrow, A. D. Stone, and K. J. Vahala, *Physical Review Letters* 100 (2008) 103905.
- [10] M. Oxborrow, in *Laser Resonators and Beam Control IX*, Vol. 6452 (A. V. Kudryashov, A. H. Paxton, and V. S. Ilchenko, eds.), SPIE, 2007.
- [11] M. Oxborrow, in *2.5-D Simulation of Axi-Symmetric Electromagnetic Structures via Weak Forms*, 2003.
- [12] R. W. Boyd, *Nonlinear Optics*, Chapter 9, Academic Press, Amsterdam ; Boston, 2008.
- [13] Pham Chi Vinh and P. G. Malischewsky, *Journal of Thermoplastic Composite Materials* 21 (2008) 337.
- [14] L. Kinsler, A. Frey, A. Coppens, and J. Sanders, *Fundamentals of acoustics*, 3 ed. (John Wiley & Sons, Inc, 1999).
- [15] D. S. Ballantine and K. L. G. Ballantine, *Acoustic wave sensors: theory, design, and physico-chemical applications*, Academic Press, San Diego, 1997.
- [16] G. Bahl, **J. Zehnpfennig**, M. Tomes, and T. Carmon, *Nature Communications*. Vol. 2, Article 403, DOI: 10.1038/ncomms1412 (2011)
- [17] **J. Zehnpfennig**, John D. 2011. *Surface optomechanics: forward and backward scattered surface acoustic waves in silica microsphere*. Thesis (Masters)--University of Michigan, 2011
- [18] **J. Zehnpfennig**, G. Bahl, M. Tomes, and T. Carmon, *Optics Express*. Vol. 19, Issue 15, pp. 14240-14248, doi:10.1364/OE.19.014240 (2011)